

Tree Containment in Multifurcating Phylogenies

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1 Introduction

The reconstruction of phylogenetic trees is one of the major computationally intense tasks in bioinformatics. However, trees are inapt at representing inter-species gene-flow, which is an important factor in the evolution of bacteria (and, in large parts, of plants) leading to the use of *networks* instead. A basic building block of this reconstruction process is the TREE CONTAINMENT problem, which asks whether a given evolutionary tree is “compatible” with a given network (can be “embedded” in the network). As this problem is well-researched for bifurcating trees and networks, it is a logical next step to try and generalize existing results to multifurcating inputs. Herein, high-degree nodes represent a lack of knowledge of the “true”, bifurcating process. Thus, multifurcating nodes can be seen as compatible with any “binary realization”.

2 Goal

The problem, called *Soft Tree Containment* (STC), is NP-hard, even on restricted classes of networks [1] for which the binary version is linear-time solvable [6, 9]. In this project, we want to attack STC (and the closely related (SOFT) CLUSTER CONTAINMENT problem) using parameterized algorithmics (see [4]). While standard parameters, like the number of horizontal transfer events (“reticulations”) in the given network, can be considered low-hanging fruit, we are curious if stronger parameterization (“level” [3], “invisible tree components” [9], “scanwidth” [2], ...) can provide a handle to solve STC on practically relevant instances. Such instances are publicly available and a contribution of independent interest could be to categorize them by the behavior of the proposed parameters. A third direction might be the search for efficient approximation or heuristic algorithms and the analysis of their proposed solution in practice. If a sufficiently interesting theoretical result can be obtained, implementation of the developed algorithm and publication in a algorithmic-focused conference or journal is desired. For further literature, see [5, 7, 8].

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